

# A Comparative Study on Direct form -1, Broadcast and Fine grain structure of FIR digital filter

Jaya Bar Madhumita Mukherjee

*Abstract-This paper presents the VLSI architecture of pipeline digital filter. The pipeline architecture is an efficient structure for designing in real time embedded system. Our work concentrates on designing digital filter using MATLAB FDA tool. Then we have implemented this filter using 3 different pipeline structure, direct form-1, broad cast and fine grain. We tested our algorithm using Xilinx synthesis tool and then implemented on Spartan 3A family XC3S700A-4fg484 FPGA device. The experimental results shows that to design an area optimized filter we should use fine grain pipeline structure, where as for high speed, we should use direct form-1 structure of digital filter.*

**Keywords-** FIR, FPGA, IIR, LTI, MATLAB, VLSI

## I. INTRODUCTION

Digital signal processing has a broad application in the field of real time signal processing operation such as speech processing, radar signal processing and different media applications[1]. These computation intensive real time application requires digital filter to perform the signal processing operation. A digital filter is an important class of linear time invariant system (LTI) that performs on a sample discrete time signal to reduce or enhanced certain aspect of that signal [2, 3]. In this paper we focus on designing low pass pipeline FIR digital filter. The general form of digital filter difference equation is given by organized as design of low pass digital filter using equation 1.

$$y(n) = - \sum_{k=1}^N a_k y(n-k) + \sum_{k=0}^{M-1} b_k X(n-k) \quad (1)$$

Where  $Y(n)$  is the current filter outputs, the  $Y(n-k)$ 's are current or previous filter inputs, the  $a_k$ 's are the filter's feed forward co-efficient corresponding to the zeros of the filter, the  $b_k$ 's are the filter's feedback co-efficient corresponding to the pole of the filter, and  $N$  is the filter's order[4,5]. Depending upon the filter co-efficient there are two type of digital filter if the co-efficient are fixed then it is frequency selective filter and if the co-efficient updated at each iteration in order to minimize the difference between the filter output and the desired signal then it is a adaptive digital filter. The frequency selective filters are of two type infinite impulse response (IIR) and finite impulse response (FIR) digital filter [6].

We have designed the low pass FIR filter using MATLAB FDA tool. Here we have developed different type of pipeline digital filter structure such as direct form1, broadcast and fine grain. For these structures we have tested our algorithm using Xilinx ISE 13.4 synthesis tools and implemented in Spartan 3A. In our paper we have proposed pipelining technique for designing the filter as in this method we can decompose the

sequential process into sub operations, with each sub process being executed in a special dedicated segment. This technique leads to reduction in critical path, power consumption and at the same time it increases the clock frequency in comparison to the parallel processing method of the designing the digital filter. The rest of the paper is MATLAB FDA tool is shown in section 2. The FPGA implementation of the direct form1 structure is given in section 3. The FPGA implementation of the broad cast structure is shown in section 4. Section 5 contains the FPGA implementation of the fine grain structure. The comparison of the optimized parameters of all designed structure is given in section 6 and section 7 contains the conclusion.

## II. DESIGN OF FIR FILTER

For signal processing operation finite impulse response (FIR) filter plays an important role, these are the digital filter that computes the output response as the weighted, finite term-sum of past, present and future values of the filter input [7] as given in equation 2.

$$y(n) = \sum_{k=M1}^{M2} b_k x(n-k) \quad (2)$$

Where  $M1, M2$  are finite. In this paper we will design a causal FIR (finite impulse response) filter; the difference equation is given as below in equation 3.

$$y(n) = \sum_{k=0}^M b_k x(n-k) \quad (3)$$

Where  $M$  is finite. To design this causal low pass filter, we will use MATLAB FDA as the synthesis tool; the specification is shown in the table 1. Depending upon the specification, we will have the transfer function co-efficient as shown in the table 2.

The magnitude and phase plot of this filter is shown in the figure 1.

We have adapted the rectangular window method to design the filter in MATLAB FDA tool. The truncated impulse response of the filter after passing through the rectangular window is given in equation 4[8].

$$h(n) = h_d(n)w_r(n)$$

$$\text{Where } w_r = \begin{cases} 1 & 0 \leq n \leq M \\ 0 & \text{otherwise} \end{cases} \quad (4)$$

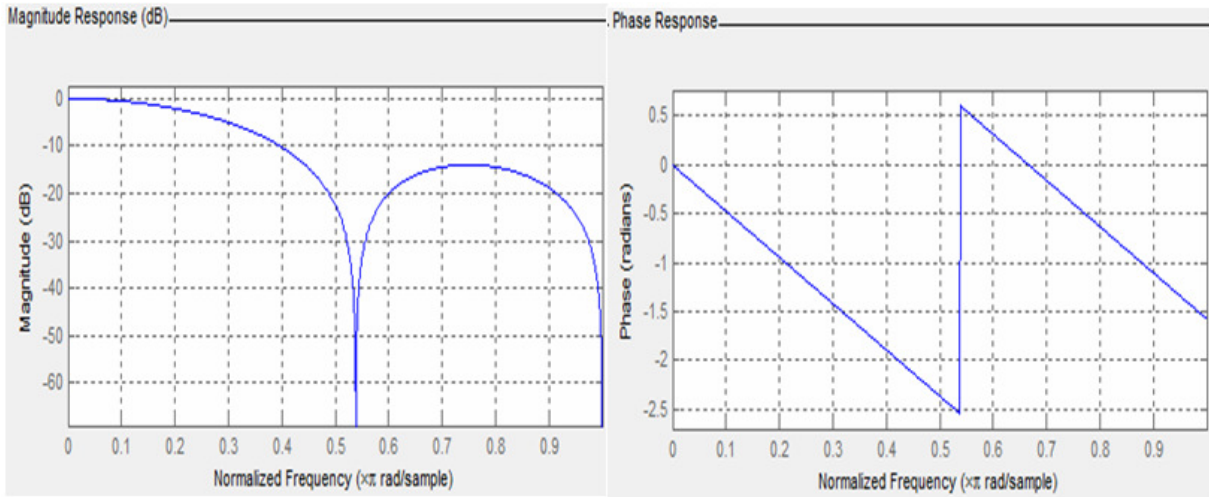


Fig.1. Magnitude and Phase plot of the filter

and  $h_d(n)$  is the impulse response of the causal FIR filter.

In frequency domain, we can represent this truncated impulse response is shown in the equation 5.

$$H(e^{j\omega}) = \frac{1}{2\pi} \int_{-\pi}^{\pi} H_d(e^{j\omega'}) w(e^{j(\omega-\omega')}) d\theta \quad (5)$$

Table 1

Properties	Specification
response	low pass
order	3 <sup>rd</sup>
table	yes
window	rectangular window
cut-off frequency ( $\omega_c$ )	0.25 (normalized)
attenuation at cut-off frequency	6 db

Table 2

Transfer function	Co-efficient
$h(0)$	0.223
$h(1)$	0.278
$h(2)$	0.278
$h(3)$	0.223

### III. IMPLEMENTATION OF FIR FILTERS USING DIRECT FORM-1 STRUCTURE

The basic Fourier transform theory states that linear convolution of two sequences in time domain is the same as the multiplication of two corresponding spectral sequence in the frequency domain [9]. Thus filtering is an essence of multiplication of signal spectrum by the frequency domain impulse of the filter. Hence according to the equation (3) of the FIR filter, we can write the output response as given in equation (6).

$$y(n) = h(0)x(n) + h(1)x(n-1) + h(2)x(n-2) + h(3)x(n-3) \quad (6)$$

According to the above equation one possible implementation structure of FIR filter is shown in the figure (2). This structure is called direct form1. Here in the branch of signal flow graph with transmittance of  $z^{-1}$  represents a delay and a branch with a transmittance of  $h(k)$  means the signal at the originating node of that branch is multiplied by a constant  $h(k)$ . For the FPGA implementation of the signal flow graph we have used the control-shift register to design the constant  $h(k)$ ,  $z^{-1}$  as the D-flip flop and ripple carry adder for the different mathematical addition operation. The simulation results with device utilization summary shown in figure below. We have implemented the filter structure in Spartan 3A family FPGA starter kit with device specification XC3S700A-4fg484, the device utilization summary and simulation waveform result is shown in figure 3 and figure 4. For FPGA implementation we have approximated our filter co-efficient the table 3, shows the deviation of the output results due to the approximation.

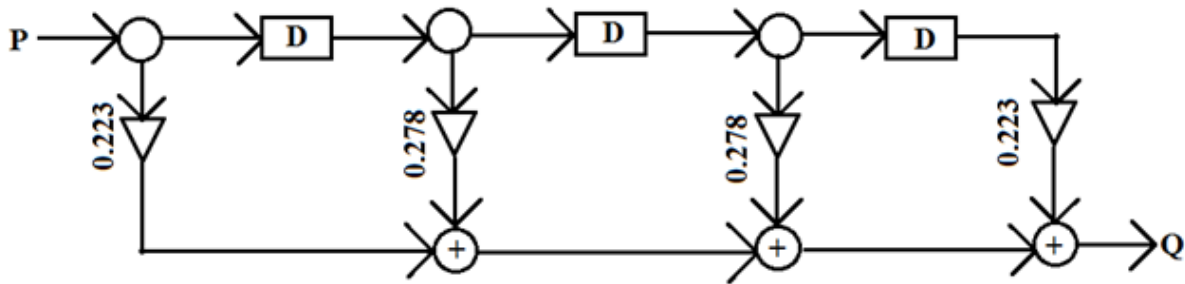


Fig.2.Direct form-1 structure of FIR filter


Device Utilization Summary				
Logic Utilization	Used	Available	Utilization	Note(s)
Number of Slice Flip Flops	41	55,296	1%	
Number of 4 input LUTs	308	55,296	1%	
Number of occupied Slices	205	27,648	1%	
Number of Slices containing only related logic	205	205	100%	
Number of Slices containing unrelated logic	0	205	0%	
Total Number of 4 input LUTs	308	55,296	1%	
Number of bonded <a href="#">IOBs</a>	31	633	4%	
Number of BUFGMUXs	1	8	12%	
Average Fanout of Non-Clock Nets	2.92			

Fig.3. Device utilization summary of the direct form-1 structure

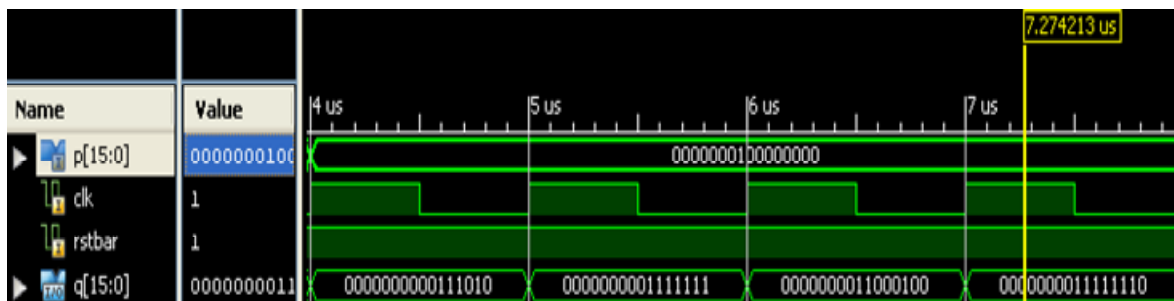


Fig4. Simulation waveform of direct form-1 structure

Table 3

<i>Input sequence</i>	1.0	1.0	1.0	1.0
<i>Actual value of output sequence(y)</i>	0.223	0.501	0.779	1.002
<i>Approximate value of output sequence (x)</i>	0.2265625	0.49609375	0.765625	0.9921875
<i>Binary equivalent value of output</i>	0000000.00111010	0000000.01111111	0000000.11000100	0000000.11111110
<i>Deviation(y-x)</i>	0.0035625	0.00490625	0.013375	0.0098125

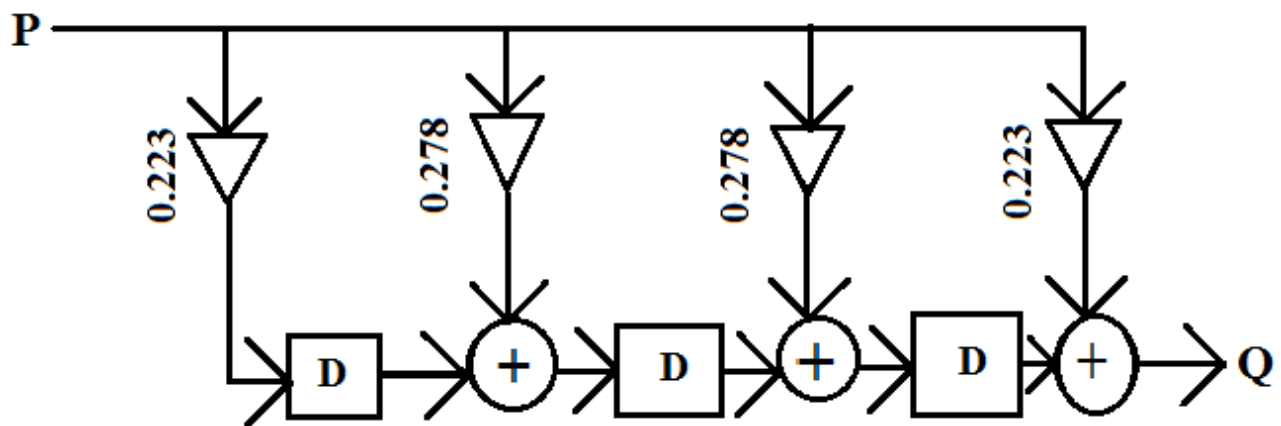


Fig.5. Broad cast structure of FIR filter

Device Utilization Summary (estimated values)				[ - ]
Logic Utilization	Used	Available	Utilization	
Number of Slices	138	27648	0%	
Number of Slice Flip Flops	46	55296	0%	
Number of 4 input LUTs	251	55296	0%	
Number of bonded IOBs	32	633	5%	
Number of GCLKs	1	8	12%	

Fig.6. Device utilization summary of the broad cast structure

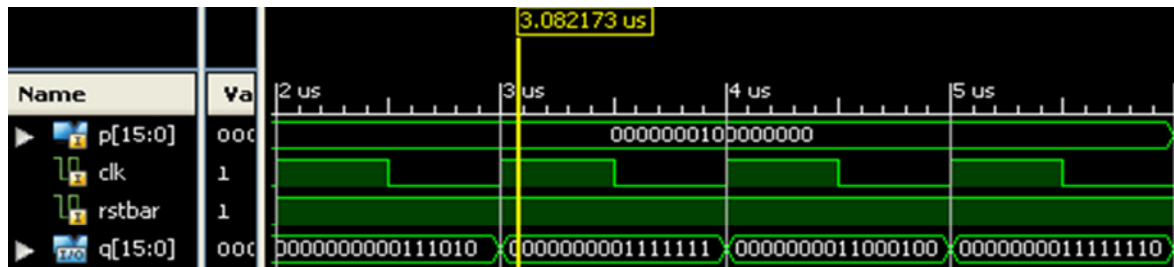


Fig.7. Simulation waveform of broad cast structure

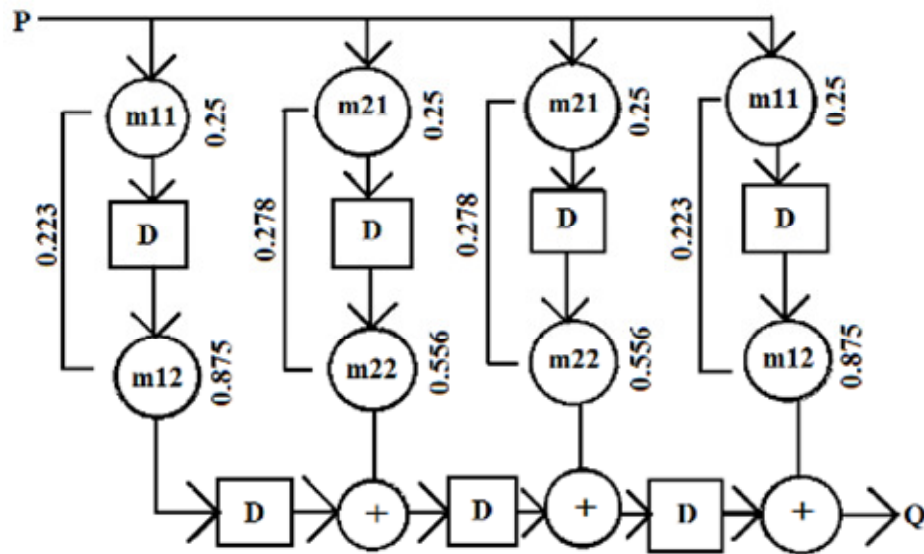


Fig.8.Fine grain structure of FIR filter

Device Utilization Summary (estimated values)			
Logic Utilization	Used	Available	Utilization
Number of Slices	123	5888	2%
Number of Slice Flip Flops	59	11776	0%
Number of 4 input LUTs	236	11776	2%
Number of bonded IOBs	31	372	8%
Number of GCLKs	1	24	4%

Fig.9. Device utilization summary of the fine grain structure

Table 4

<i>Input sequence</i>	1.0	1.0	1.0	1.0
<i>Actual value of output sequence(y)</i>	0.223	0.501	0.779	1.002
<i>Approximate value of output sequence (x)</i>	0.21875	0.49675	0.77475	0.9935
<i>Binary equivalent value of output</i>	00000000.00111000	00000000.01111111	00000000.11000110	00000000.11111110
<i>Deviation(y-x)</i>	.00425	.00425	.00425	.0085

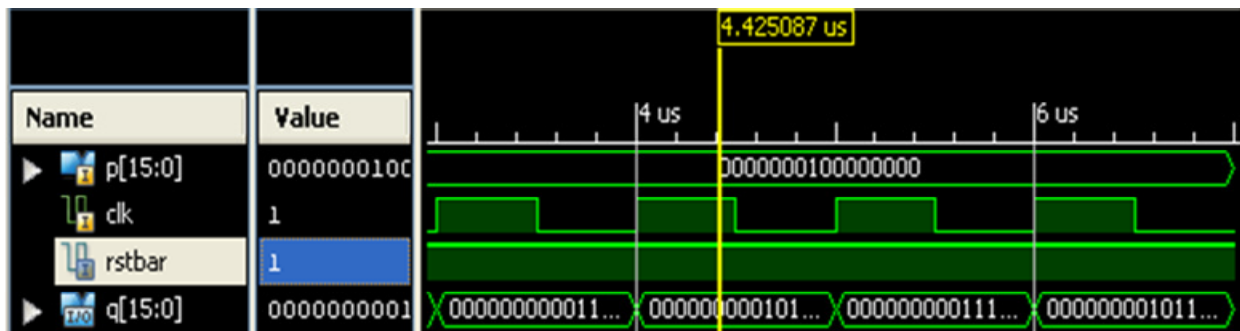


Fig.10. Simulation waveform of fine grain structure

#### IV. IMPLEMENTATION OF FIR FILTERS USING BROAD CAST STRUCTURE

We can transform a given system into a different network structure while maintaining the same system function. One of such transformation is the transposition technique. In this theorem we reverse the direction of all the branches, at the same time we interchange input and output. If we apply transposition theorem to the direct form-1 structure of FIR filter we can obtain the broad cast structure. The figure 5 shows the broad cast structure. For the FPGA implementation of this structure we have design shift register, ripple carry adder and D-flip flop as we have done for the direct form-1 structure. The simulation result and the device utilization summary are given in figure 6 and figure 7, for this structure.

#### V. IMPLEMENTATION OF FIR FILTERS USING FINE GRAIN STRUCTURE

Fine grain pipelining is a technique of decomposing the computation intensive multipliers into small segments. In this method a delay unit is inserted in the small segment of the multiplier so that the critical path and the execution time can be reduced [10]. This structure has a disadvantage that due to the insertion of pipeline latches the area requirement for such structure becomes more in comparison to other structure. The fine grain structure for our low pass FIR filter is shown in the figure 8. Due to the approximation of the multiplier unit there is a deviation of the output response. The table 4 has shown the deviated output response. For the FPGA implementation of this structure, the simulation result and device utilization summary is shown in the figure 9 and figure 10.

#### VI. COMPARISON

This section presents some comparison results of the proposed architecture of pipeline digital FIR filter. Here we compare direct form-1, broad cast and fine grain structure depending upon the utilization of slice, sliced flip-flop and 4 input LUTs. The graphical analysis result is shown in figure 11.

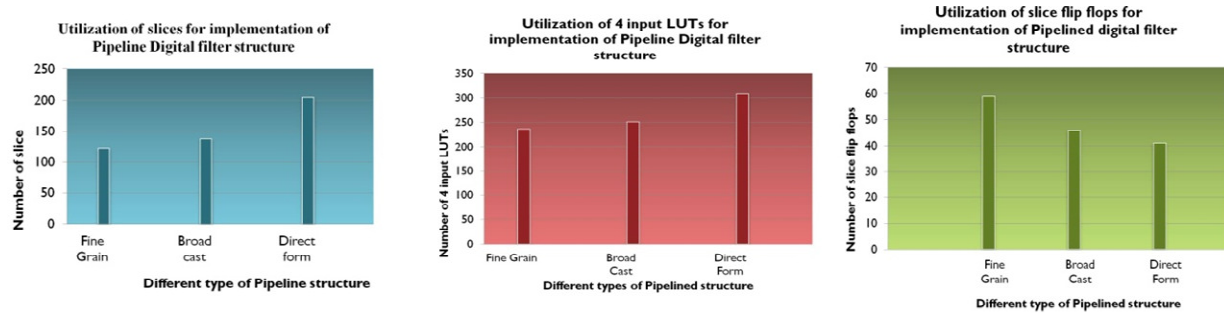


Fig.11.Comparison table

## CONCLUSION

In this paper we have proposed three structure of pipeline digital filter. Our main aim in this paper is to design an area optimized high speed pipeline digital FIR filter. The implementation results shows that for an area optimized filter we should use fine grain pipeline structure, where as to design a high speed digital filter we should use direct form-1 structure as it has maximum operating frequency.

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## AUTHOR'S PROFILE

	<p><b>Jaya Bar</b></p> <p>Received B.Tech degree from Camellia Institute of Technology (West Bengal University of technology) in 2011 and pursuing M.Tech from Heritage Institute of technology (West Bengal University Of Technology). Her research interest include embedded system, Digital signal processing and VLSI architecture.</p> <p><a href="mailto:jayabar01@gmail.com">jayabar01@gmail.com</a></p>
	<p><b>Madhumita Mukherjee</b></p> <p>Received B.Tech degree from West Bengal University of Technology in 2007 and M.Tech from Jadavpur University in 2011 respectively. she is currently Assistant Professor in department of Electronics and Telecommunication on Heritage Institute of Technology under West Bengal University of Technology. Her research interest include embedded system, Digital signal processing and VLSI architecture.</p> <p><a href="mailto:madhumita.mukherjee@heritageit.edu">madhumita.mukherjee@heritageit.edu</a></p>